



**Requests to theorists
from experimentalists**

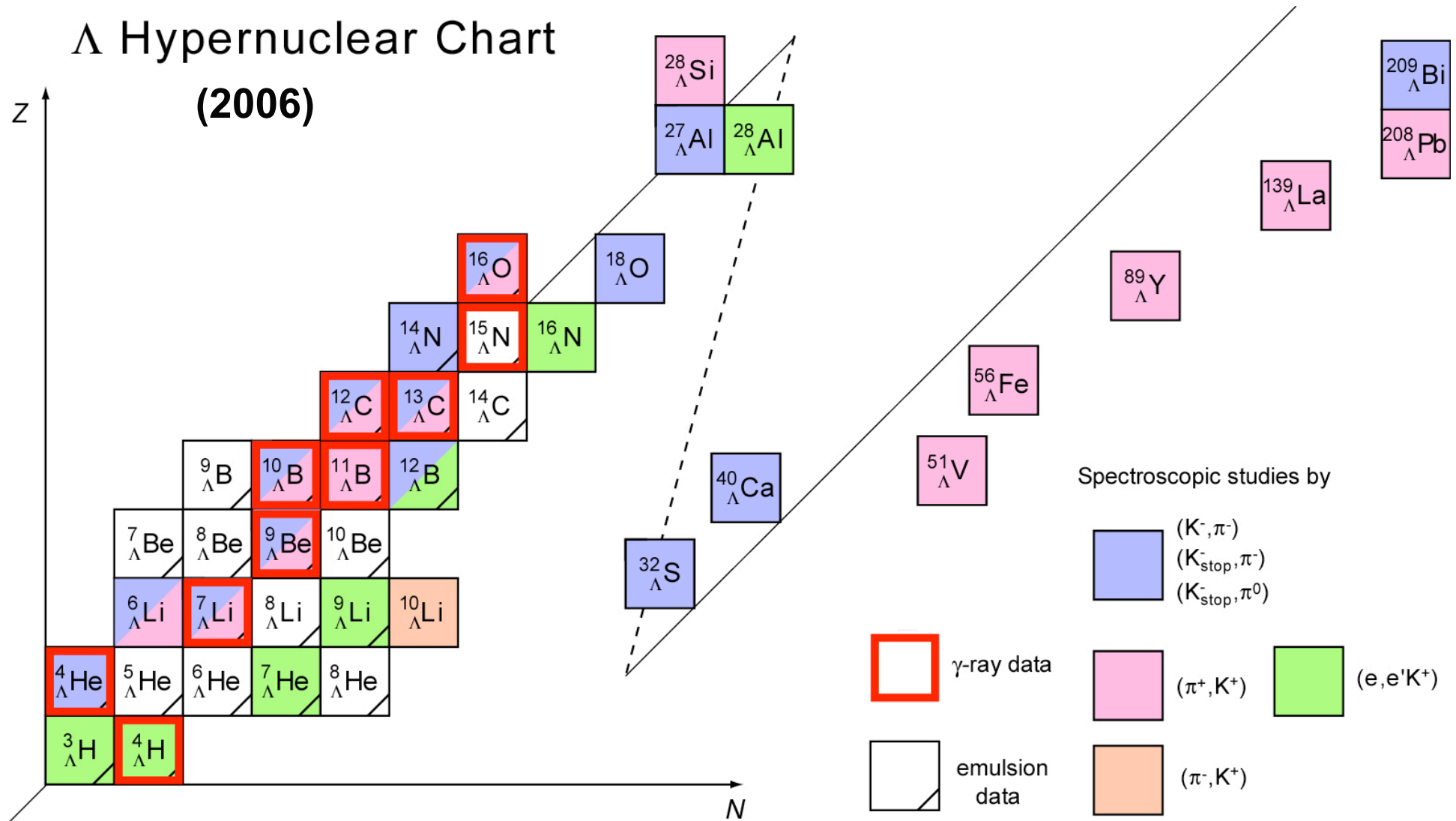
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H. Tamura**

Experimental status and plans

Experimental plans (2009~2019)

- Λ hypernuclear structure
 - $(e, e'K^+)$: $A=7\sim 89$, $\Delta E = 400$ keV (FWHM)
 - γ spectroscopy: $A=4\sim 208$, $B(M1)$, $B(E2)$, n-rich,..
 - (π^-, K^+) n-rich: ${}^6_{\Lambda}\text{H}$, ${}^9_{\Lambda}\text{He}$, ...
 - High-resolution (π^\pm, K^+)
 - HI induced reaction: p-rich/n-rich
- Ξ hypernuclear spectroscopy: U_{Ξ} , W_{Ξ} , $\Xi\text{N}-\Lambda\Lambda$ mixing
- $\Lambda\Lambda$ hypernuclei: $B_{\Lambda\Lambda}$ and decay
- Ξ atomic X-rays
- Σ hypernuclei/ Σ -nuclear systems
- Weak decays
- ΛN , ΣN , (ΞN) scattering

Present Status of Λ Hypernuclear Spectroscopy



Updated from: O. Hashimoto and H. Tamura, Prog. Part. Nucl. Phys. 57 (2006) 564.

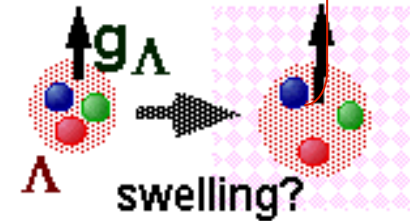
J-PARCでのガンマ線分光のテーマ(例)

- Λ N 相互作用の詳細 (E13)

- Charge symmetry breaking ${}^4_{\Lambda}\text{He}(1^+-0^+)$
- Λ N スピン依存相互作用と Λ NN force ${}^{10}_{\Lambda}\text{B}$ and ${}^{11}_{\Lambda}\text{B}$
- Λ N 相互作用の動径依存性 ${}^{19}_{\Lambda}\text{F}$

J-PARC E13

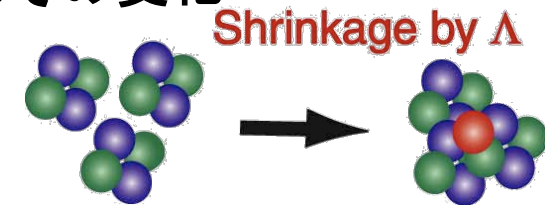
- B(M1) 測定 -> 核内 Λ のg因子の変化 ${}^7_{\Lambda}\text{Li}$



- B(E2) 測定

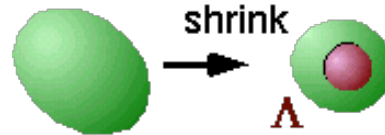
${}^9_{\Lambda}\text{Be}$ and ${}^{13}_{\Lambda}\text{C} \rightarrow {}^8\text{Be}, {}^{12}\text{C}$ のクラスター構造と Λ によるその変化

${}^7_{\Lambda}\text{He} \rightarrow {}^6\text{He}$ の中性子ハローの消失



- sd-殻ハイパー核

→ 変形、集団運動の変化



- 重い Λ ハイパー核 ${}^{89}_{\Lambda}\text{Y}$, ${}^{208}_{\Lambda}\text{Pb}$, etc.

→ Λ 核ポテンシャルの詳細、核内深部のバリオンの性質
(s_{Λ} - p_{Λ} energy, p_{Λ} LS splitting, B(M1))

Interaction Parameters (Millener)

$$\Delta E = -0.04\Delta + 2.46S_{\Lambda} + 0.99T$$

S_N : consistent

$S_{\Lambda} = -0.01 \text{ MeV}$

$\Delta < 0.3 \text{ MeV}$

Δ, S_{Λ}, T : consistent

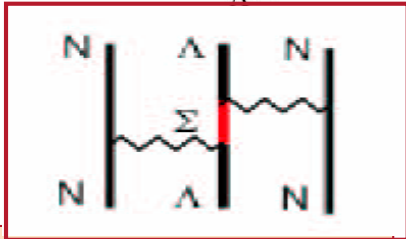
$S_N = -0.4 \text{ MeV}$

$$\Delta E = 0.70S_N$$

$\Delta = 0.43 \text{ MeV}$

$$\Delta E = 1.44\Delta + 0.05S_{\Lambda} - 0.27T$$

S_N : consistent



Effect of ΣN - ΛN coupling force?
Accuracy of core wave function?

$\Delta, S_{\Lambda}, S_N, T$ determined.
Consistency almost OK.

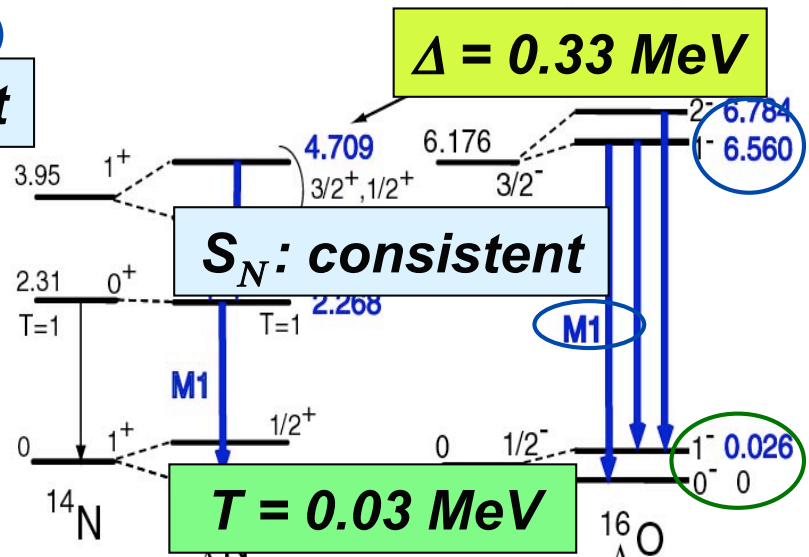
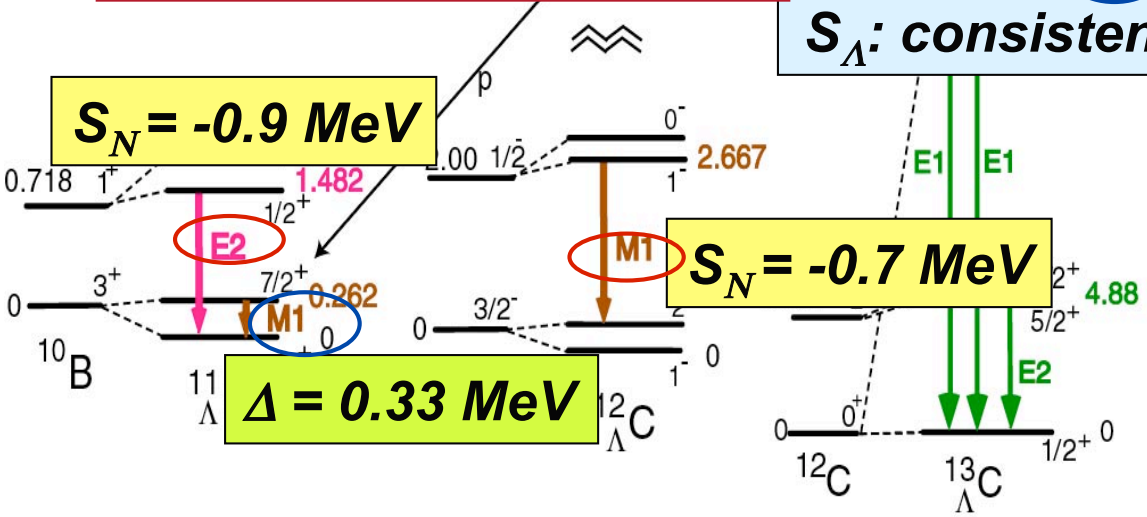
S_{Λ} : consistent

$\Delta = 0.33 \text{ MeV}$

$S_N = -0.9 \text{ MeV}$

$S_N = -0.7 \text{ MeV}$

$\Delta = 0.33 \text{ MeV}$



$$\Delta E = -0.38\Delta + 1.38S_{\Lambda} + 7.85T$$

$T = 0.03 \text{ MeV}$

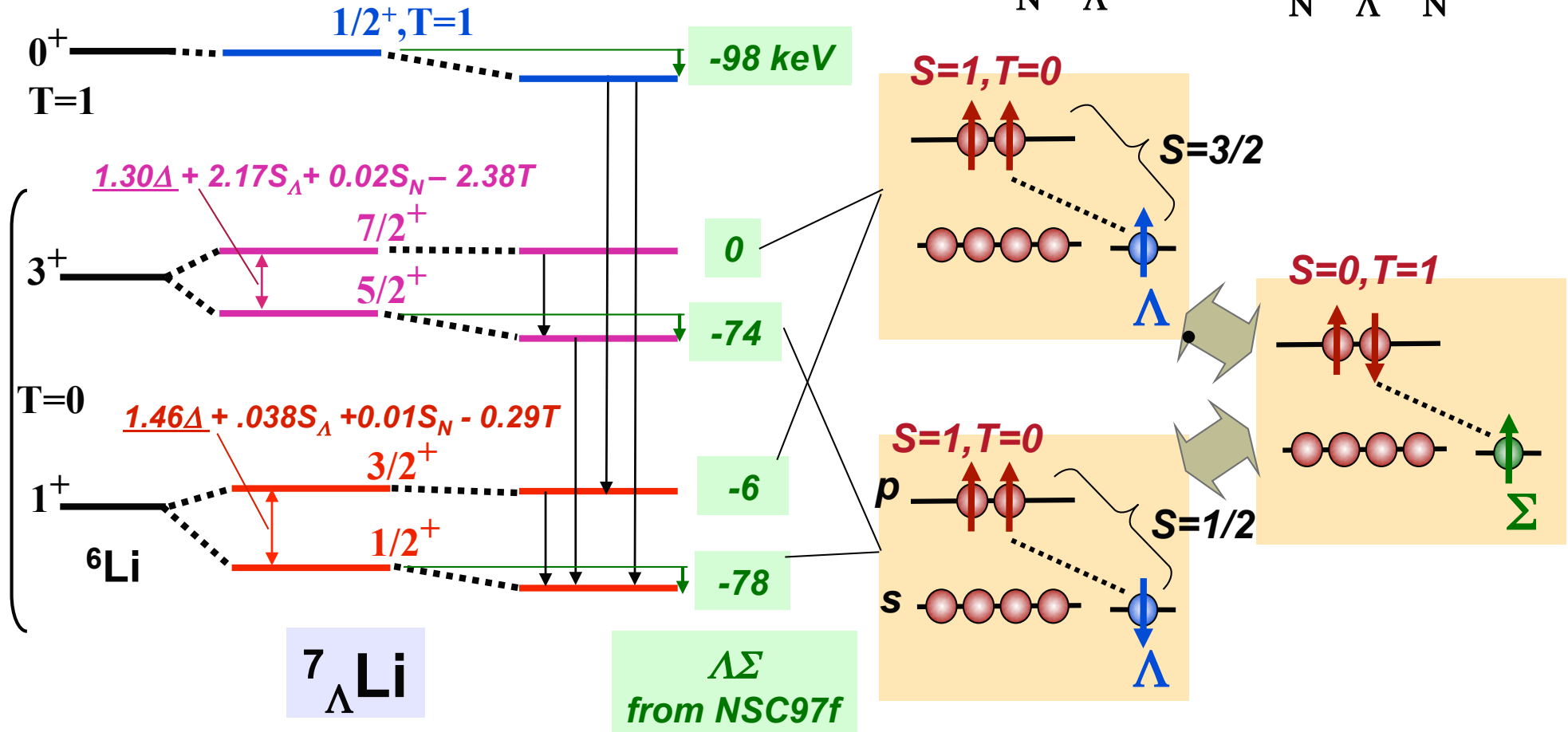
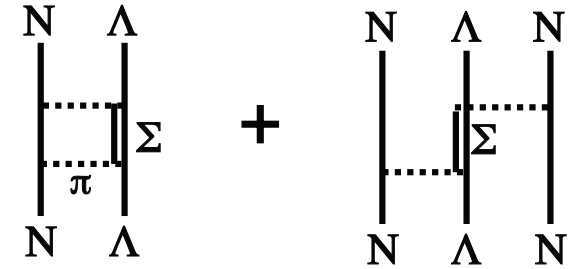
Millener's approach for ΛN - ΣN coupling

Millener, *Lecture Notes in Physics 724, Springer (2007) p.31*

$$v = \langle p_N^{A-5} s_\Sigma(J) | V | p_N^{A-5} s_\Lambda(J) \rangle \quad V: \text{NSC97f through G-matrix (spin-dependent)}$$

$$\text{Energy shift } (\Delta\Sigma) = v^2 / (m_\Sigma - m_\Lambda)$$

($s_N^4 s_\Sigma - s_N^4 s_\Lambda$ coupling has no spin-dependence and can be incorporated in effective 2B ΛN force.)



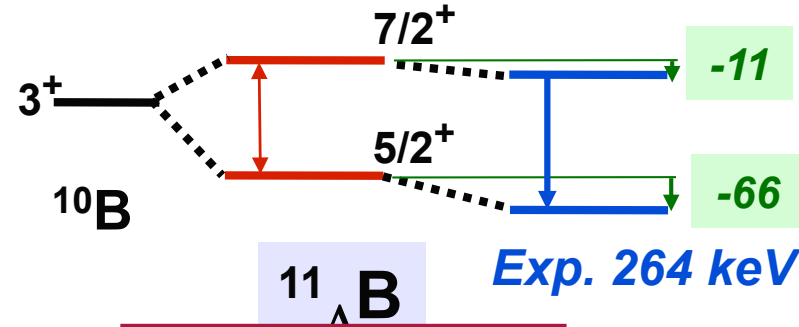
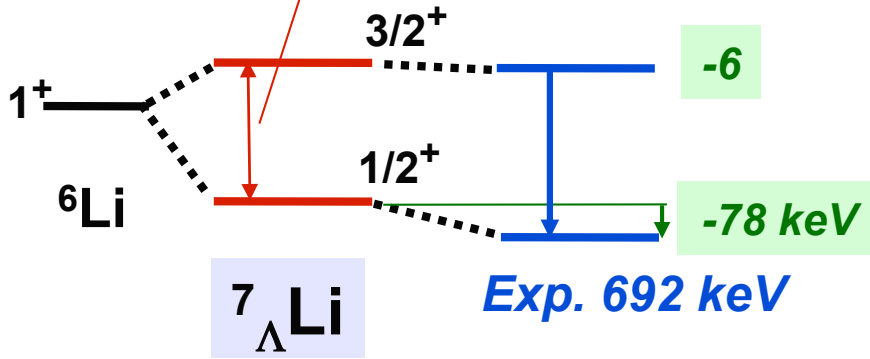
Spin-spin strength (Δ) and Λ - Σ coupling (Millener)

$\Lambda\Sigma$
from NSC97f

$S_\Lambda = -0.01$ MeV, $T = 0.03$ MeV from exp.

$1.46\Delta + .038S_\Lambda + 0.01S_N - 0.29T$

$1.03\Delta + 2.47S_\Lambda + 0.03S_N - 3.36T$



w/o $\Lambda\Sigma$: $\Delta = 0.50$ MeV

w/ $\Lambda\Sigma$: $\Delta = 0.43$ MeV

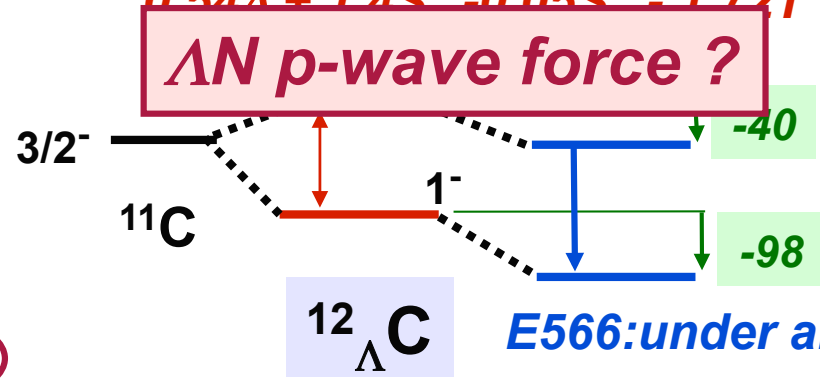
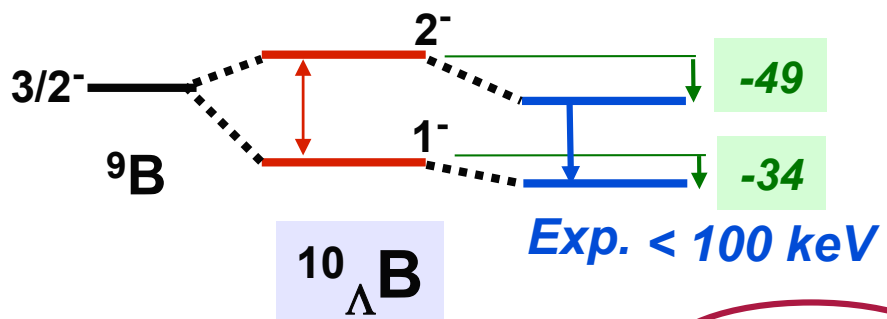
Size Effect ?

$\Delta = 0.33$ MeV

$\Lambda\Sigma$ is correct ?

$0.58\Delta + 1.41S_\Lambda - 0.01S_N - 1.07T$

$0.54\Delta + 1.4S_\Lambda - 0.05S_N - 1.72T$



ΛN p-wave force ?

$\Delta < 0.3$ MeV

核内 Λ のg因子測定

核内バリオンの磁気モーメント

カイラル対称性の部分的回復の影響を受けるか？

→ バリオンのスピンの起源、質量の起源と深く関連

核内 μ_Λ → バリオンの核媒質効果を見る

■ 直接測定は極めて困難 ($\tau \sim 0.1 - 0.2$ ns)

■ Λ -spin-flip M1 遷移の $B(M1) \rightarrow g_\Lambda$

$$B(M1) = (2J_{up} + 1)^{-1} |\langle \Psi_{low} \| \mu \| \Psi_{up} \rangle|^2$$

$$= (2J_{up} + 1)^{-1} |\langle \Psi_{\Lambda\downarrow} \psi_c \| \mu \| \Psi_{\Lambda\uparrow} \psi_c \rangle|^2$$

$$\mu = g_c \mathbf{J}_c + g_\Lambda \mathbf{J}_\Lambda = g_c \mathbf{J} + (g_\Lambda - g_c) \mathbf{J}_\Lambda$$

$$= \frac{3}{8\pi} \frac{2J_{low} + 1}{2J_c + 1} (g_\Lambda - g_c)^2 \quad [\mu_N^2]$$

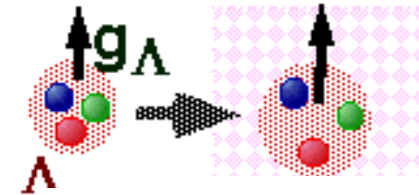
~100% **Doppler Shift Attenuation Method :**

$$\Gamma = BR / \tau = \frac{16\pi}{9} E_\gamma^3 B(M1)$$

Applied to “hypernuclear shrinkage”
in ${}^7_\Lambda\text{Li}$ from B(E2): *PRL* 86 ('01)1982

$$\mu_q = \frac{e\hbar}{2m_q c} \quad m_q : \text{Const. quark mass}$$

m_q が減少 → μ_q 増大？



swelling → μ_q 増大？

g_c

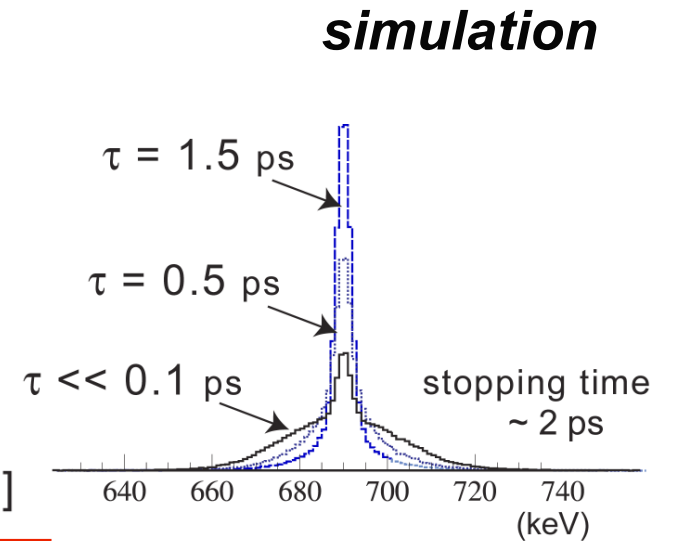
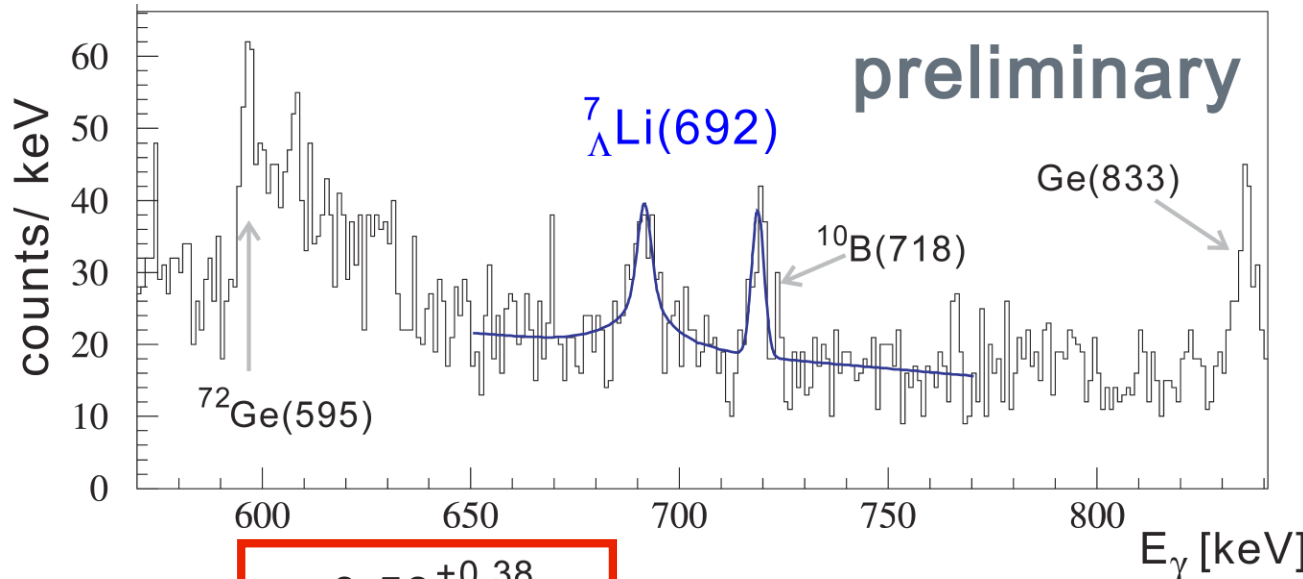
$\Psi_{\Lambda\uparrow} \psi_c$



$\Psi_{\Lambda\downarrow} \psi_c$

Preliminary data on B(M1) in ${}^7_{\Lambda}\text{Li}$ (BNL E930)

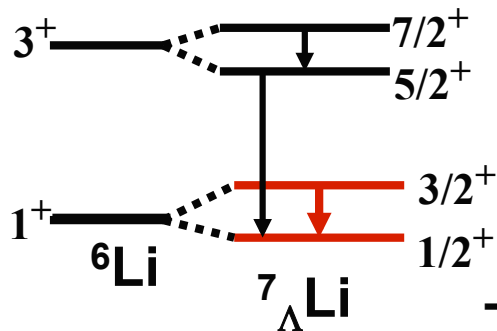
${}^{10}\text{B} (K^-, \pi^-) {}^{10}_{\Lambda}\text{B}^*$, ${}^{10}_{\Lambda}\text{B}^*(3^+) \rightarrow {}^7_{\Lambda}\text{Li}^*(3/2^+) + {}^3\text{He}$ indirect population



$$\tau = 0.58^{+0.38}_{-0.20} \text{ ps}$$

$$\text{BR}(M1) = 100\%$$

$$B(M1) = 0.30^{+0.12}_{-0.16} [\mu_N^2]$$



$$-g_{\Lambda} = 1.1^{+0.4}_{-0.6} \mu_N$$

preliminary
(statistical error only)

$$\leftrightarrow -g_{\Lambda}(\text{free}) = 1.226 \mu_N$$

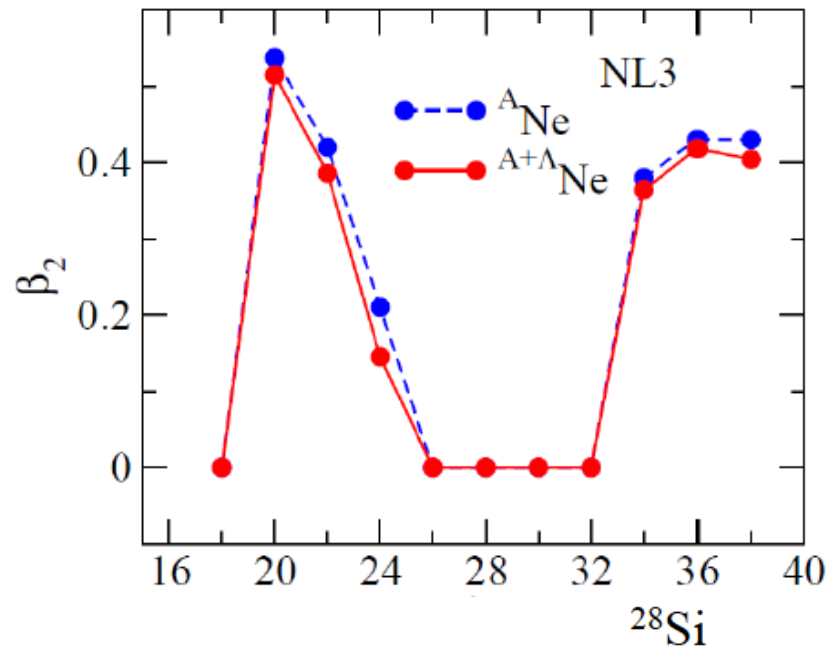
First data of g_{Λ} in nucleus

-> Precise B(M1) measurement of ${}^7_{\Lambda}\text{Li}$ at J-PARC

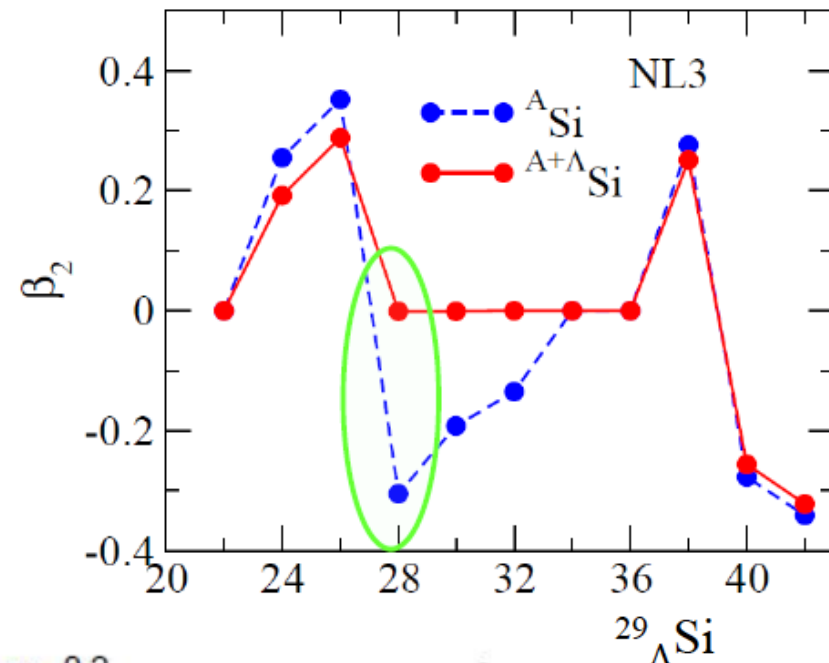
J-PARC E13 (Tamura et al.)

Impurity effect in deformation (Hagino)

Ne isotopes

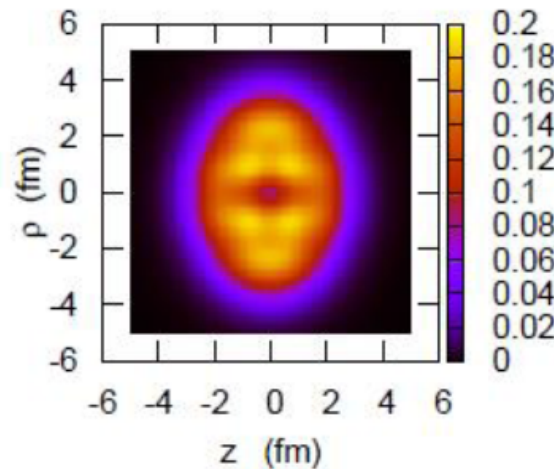


Si isotopes

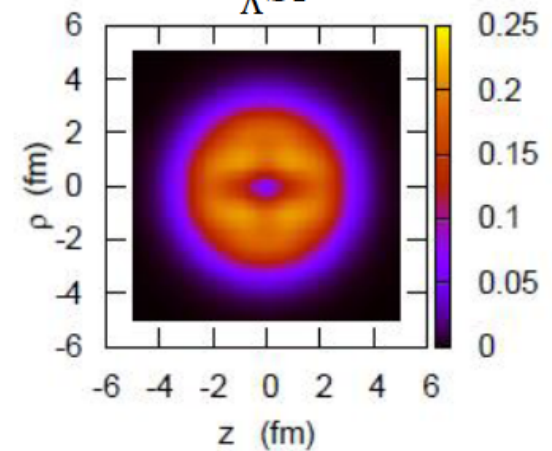


- in most cases, the hypernucle
 - hypernuclei: sl
- conc

Exception: $^{29}_{\Lambda}\text{Si}$



Λ



Myaing Thi Win and K.H., PRC78('08)054311

Requests to theorists

Λ hypernuclear structure

- **Need for shell-model description better than Millener's ($s^4 p^{A-5} s_\Lambda$)**
 - Need for larger shell model space and better core wave functions
 - Distinguish effects of 2B and 3B interactions from ΛN - ΣN ?
(The 2-body ΛN - ΣN coupling force is incorporated in the effective ΛN interaction. Double counting?)
 - Effect of ΛN - ΣN coupling with s^4 nucleons ?
 - Important (*Nemura et al. PRL 89 (2002) 142504*) but incorporated in 2BF?
 - Relation between BB interaction models and the parameters
- **Need for Few-body calc. with $\Lambda\Sigma$ coupling for p-shell (${}^7_\Lambda\text{Li}$, ${}^{10}_\Lambda\text{B}$, ${}^{11}_\Lambda\text{B}$)**
 - Cluster model calculations with ΛN - ΣN coupling
 - Ab initio calculation (Quantum Monte Carlo...) possible?
 - Extract contributions of p-wave force
 - Inclusion of tensor force (for p1/2 shell hypernuclei?)
- **Radial dependence of ΛN int. from sd-shell structure?**
- **How to extract info. on ΛNN force from n-rich hypernuclei?**
- **Collective motion in sd shell hypernuclei (mean-field approach)**

Other issues in Λ hypernuclei

- **B(M1) for ${}^7_{\Lambda}\text{Li}$**
 - Effect of “core polarization”
 - Effects of meson exchange current and Σ mixing
 - **Effect of partial restoration of chiral symmetry**
 - ${}^{12}_{\Lambda}\text{C}$ and other hypernuclei
- **Charge Symmetry Breaking (どちらかというと実験待ち)**
 - ${}^4_{\Lambda}\text{H}$ - ${}^4_{\Lambda}\text{He}$ with recent BB interactions
 - $A=7, A=12 \dots$ (e,e' K^+) data (will be) available.
- **Medium/Heavy hypernuclei**
 - B_{Λ} , m^*_{Λ} , s_{Λ} - p_{Λ} in heavy hypernuclei -> then what can we see?
 - How LS splitting appears in large A ?
 - B(M1) in heavy hypernuclei

Weak decays

- **Asymmetry puzzle – solved? μ can be measured?**
- **$\Lambda NN \rightarrow NNN$: What is new? (Bhang)**
- **Direct quark process unnecessary in NMWD?**
What is the unified picture of BB interaction?
- **$\Delta I=1/2$ rule (${}^4_{\Lambda}\text{H}$, ${}^4_{\Lambda}\text{He}$ exp.) (Ajimura)**
- **π^+ decay should be measured?**
- **$\Lambda\Lambda \rightarrow \Sigma N$, ΛN decay: How is the relation to H-dibaryon correlation in nucleus?**
- **Semi-leptonic decay $\Lambda \rightarrow p e^- \nu_{\text{bar}}$, $\Lambda \rightarrow p \mu^- \nu_{\text{bar}}$ BR $\sim 10^{-3}$**
-> Possible change of baryon property
How sensitive to wave function of s/u quark in nucleus?
(Also sensitive to Pauli effect...)

実験施設充実のために必要な検討

- **K1.1 ライン** (補正でできるかも) **for (K^- , π^-)**
 - **ガンマ線分光 (sd-shell, medium-heavy)**
-> 集団運動の不純物効果、核内 Λ の性質変化
どれくらいの効果が期待できるか？ ポテンシャルの詳細と核内 Λ の性質変化の関係は？
 - **ΣN , ΛN scattering** 測定精度と相互作用モデルの判別性は？
 - **少数系 Σ 核** -> ΣN 相互作用の(T,S)ごとの強さ
どれくらいの精度で強さが決まるのか？
 - **Θ 核, weak decay, ...**
- **High-Resolution pion line (Noumi line)**
20億円 + ホール拡張 (80億円)
 - **(π^\pm , K^+) 高分解能 (~200 keV FWHM) 分光**
-> (中重) Λ 核、中性子過剰 Λ 核、 Σ 核、(weak decay)
何がどこまでわかるのか？ インパクトは？
他に使い道は？

G-matrix results for various interactions

Rijken et al., PRC59 (1999) 21

TABLE XIV. Contributions to U_{Σ} at $k_F=1.0 \text{ fm}^{-1}$ in the cases of NSC97e, NSC97f, NSC89, NHC-F, and NHC-D. Conversion widths Γ_{Σ} are also shown. All entries are in MeV.

| Model | Isospin $T=\frac{1}{2}$ | | | Isospin $T=\frac{3}{2}$ | | | Sum | Γ_{Σ} |
|-------------|-------------------------|---------|------|-------------------------|---------|-------|-------|-------------------|
| | 1S_0 | 3S_1 | P | 1S_0 | 3S_1 | P | | |
| NSC97e | 5.2 | -7.5 | 0.0 | -6.1 | -2.5 | -0.9 | -11.8 | 14.6 |
| NSC97f | 5.2 | -7.6 | 0.0 | -6.2 | -2.2 | -0.9 | -11.6 | 15.5 |
| NSC89 | 3.0 | -4.2 | -0.3 | -5.8 | 3.7 | 0.1 | -3.6 | 25.0 |
| NHC-F | 4.2 | -10.9 | -1.5 | -5.3 | 18.6 | -1.7 | 3.5 | 16.3 |
| NHC-D | 2.1 | -9.6 | -2.2 | -5.4 | 9.4 | -3.0 | -8.7 | 8.7 |
| ESC04d | 6.5 | -21.0 | -3.4 | -20.2 | 24.0 | -20.9 | -26.0 | |
| fss2(quark) | 6.7 | -23.9 | -5.2 | -9.2 | 41.2 | -1.4 | 7.5 | |

Rijken, Yamamoto
PRC73 (2006) 044008

Fujiwara et al.,
Prog.Part.Nucl.Phys.
58 (2007) 439
 $k_f=1.35 \text{ fm}^{-1}$

Lane term $(\sigma_{\Sigma}\sigma_N)(\tau_{\Sigma}\tau_N)$ by π/ρ exchange quark Pauli effect

Previous ${}^3\text{He}(K^-, \pi^-)$ data at BNL E774

R.S. Hayano / ${}^4\text{He}(K^-, \pi^\pm)$ experiments at KEK and BNL

155c

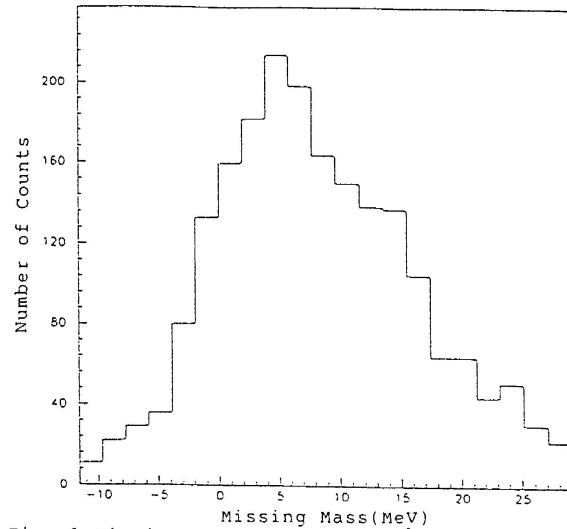


Fig. 1 Missing Mass Spectrum of ${}^3\text{He}(K^-, \pi^+)$ reaction.

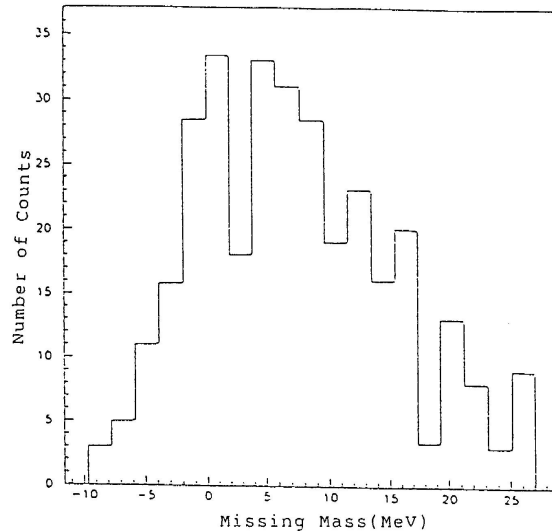
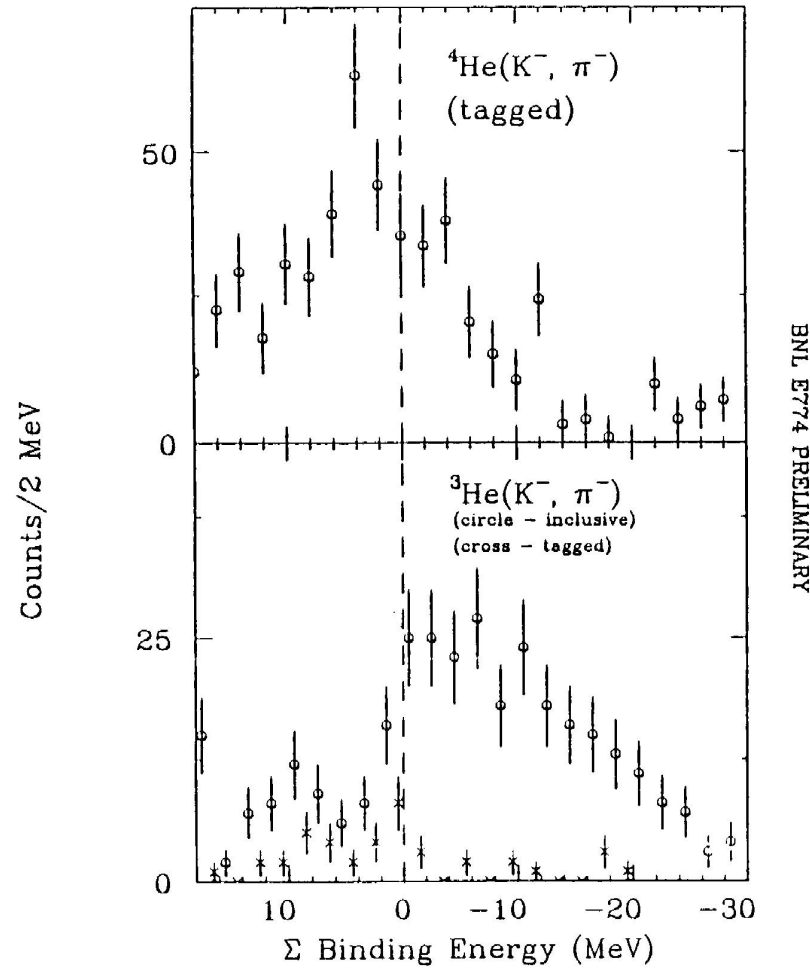


Fig. 2 Missing Mass Spectrum as in fig. 1 but with multiplicity 2 cut.



Top: ${}^4\text{He}(K^-, \pi^-)$ data tagged with the multiplicity ≥ 2 condition (same as in Fig. 1). Bottom: ${}^3\text{He}(K^-, \pi^-)$ spectra. Inclusive data are in open circles and multiplicity-tagged data are in crosses.

Proposed ^3He experiment

- ^3He ($\text{K}^-, \pi^{\pm,0} \Lambda$) at threshold, $p_{\text{K}} \sim 0.5 \sim 0.6 \text{ GeV}/c$ ($q < 50 \text{ MeV}/c$)
- $^3_{\Sigma}\text{He}$, $^3_{\Sigma}\text{H}$, $^3_{\Sigma}\text{n}$: different combination of
 $(T_{\text{N}\Sigma}, S_{\text{N}\Sigma}) = (3/2, 1), (3/2, 0), (1/2, 1), (3/2, 0)$ from $^4_{\Sigma}\text{He}$, $^4_{\Sigma}\text{n}$
- 3-body systems can be accurately calculated
 -> direct comparison with various interactions
 (how sensitive? – theoretical calculations essential)
- Apparatus: Low momentum beam line (K1.1BR)
 + beam spectrometer + SPESII and π^0 spectrometer + Λ tagger (CDS)

Koike-Harada (NPA611(1996)461) “Unstable bound states”

| $E_{\Sigma}(\Gamma)$ | SAP-1(ND) | SAP-F(NF) |
|---|--------------|------------------|
| $^3_{\Sigma}\text{He} (T=1, S=1/2)$ | --- | +1.77 (7.58) MeV |
| $^3_{\Sigma^0}\text{H} (T \sim 1, S=1/2)$ | +0.01 (1.95) | +0.63 (8.2) MeV |
| $^3_{\Sigma}\text{n} (T=1, S=1/2)$ | --- | +0.55 (9.05) MeV |

Spectral shapes should be calculated.

Experiment

- Beam spectrometer ($\Delta p_{FWHM} < 1.5 \text{ MeV/c}$ at 600 MeV/c)
in place of K1.1BR B3
- ^3He target
- Λ tagger => CDS
- π^\pm spectrometer ($\Delta p_{FWHM} < 1.5 \text{ MeV/c}$ at 500 MeV/c)
=> SPESII
- π^0 spectrometer ($\Delta p_{FWHM} \sim 3 \text{ MeV/c}$ at 500 MeV/c)

Yield (K^- , π^\pm): $N_{K^-} \cdot d\sigma/d\Omega \cdot \Delta\Omega \cdot N_{\text{target}} \cdot \varepsilon(\Lambda\text{tag}) \cdot \varepsilon$

$$= 5 \times 10^5 / \text{spill} \cdot 50 \times 10^{-30} \text{ cm}^2 / \text{sr} \cdot 0.02 \text{ sr} \cdot 0.09 \text{ g/cm}^3 / 3 \cdot 10 \text{ cm} \cdot 6 \times 10^{23} \cdot 0.3 \cdot 0.5$$

=> 1400 counts/100hours -> *Lower beam momentum?*

Yield (K^- , $\pi^{\pm 0}$):

=> ~100 counts/100hours